

Modeled Integrated Scattering Tool (MIST)

Version 2.30

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The MIST program has been developed to provide users with a general application to model an integrated scattering system. The program performs an integration of the bidirectional reflectance distribution function (BRDF) over solid angles specified by the user and allows the dependence of these integrals on model parameters to be investigated. The models are provided by the SCATMECH library of scattering codes. Version 2.00 adds a user-friendly Windows interface, enabling visualization of results, browsing of models, and automated parameter generation.

1. Introduction

Light scattering is widely used by scanning surface inspection tools to inspect materials, such as silicon wafers, flat panel display substrates, data storage media, and optics, for defects, particles, and surface roughness. These instruments often direct collimated or lightly-focused light at a sample and collect scattered light with one or more large optics. The optics collect light over significant solid angles in order to maximize sensitivity. When designing these instruments, it helps to be able to predict the signal for different geometric conditions and model parameters.

The BRDF characterizes the directional dependence of the scattering by a material. The BRDF is given by

$$f_r(\theta_i, \theta_s, \phi_s) = \lim_{\Omega \rightarrow 0} \frac{\Phi_s}{\Phi_i \Omega \cos \theta_s}, \quad (1)$$

where Φ_s is the power scattered into solid angle Ω , centered on polar angle θ_s and azimuth angle ϕ_s , and Φ_i is the power incident on the sample at an angle θ_i . The angles θ_i , θ_s , and ϕ_s are defined in Fig. 1. The function $f_r(\theta_i, \theta_s, \phi_s)$ also depends upon the polarization state of the incident light and the polarization sensitivity of the detection system. Any optic collecting light over a finite solid angle measures a reflectance given by

$$\rho(\Omega) = \int_{\Omega} f_r(\theta_i, \theta_s, \phi_s) \cos \theta_s d\Omega. \quad (2)$$

If we make a change of variables, $\xi = \theta_s \cos \phi_s$ and $\eta = \theta_s \sin \phi_s$, then Eq. 2 becomes

$$\rho(\Omega) = \int_{\Omega} f_r(\theta_i, \theta_s, \phi_s) \cos \theta_s \sin \theta_s d\xi d\eta \quad (3)$$

Eq. (3) is slightly easier to use than Eq. (2), since the differentials can be made more uniform over the collection aperture.

The MIST program uses theoretical models for the BRDF which are supplied by the SCATMECH library and calculates the quantity $\rho(\Omega)$ using Eq. (3) for geometries specified by the user. Furthermore, MIST allows the user to vary parameters in the model or in the definition of the solid angle, providing the user with the dependences on those parameters.

Besides using it as a design tool, one application of MIST is the development of calibration curves for an instrument. For example, the absolute response of an instrument to spherical particles can be accurately determined as a function of the particle size using the SCATMECH model

Bobbert_Vlieger_BRDF_Model. If a set of reference particles are used to calibrate the instrument, then these calibration curves can be used to interpolate (or even extrapolate) to other particle sizes. The advantage of using a model-based calibration curve, over using non-physically-based interpolation techniques, is that it is more accurate and the calibration should not change if the set of reference particles changes. Furthermore, a smaller number of reference particles are needed for calibration, and over sampling of the calibration curve provides information about uncertainties in the measurement and can compensate for uncorrelated uncertainties in the reference particle diameters.

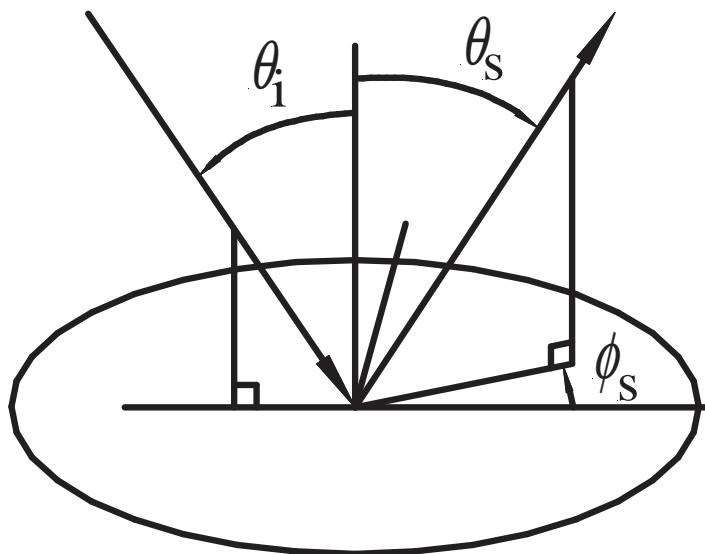


FIGURE 1 The scattering geometry and angle convention used by the calculations. The incident angle is θ_i . The scattering direction is defined by polar angle θ_s and azimuth angle ϕ_s .

2. Installing MIST

The MIST software package is supplied in a self-extracting executable file (**MISTzip220.exe**). To install the software, the user should run **mistzip220.exe** from a temporary directory. The program will create a directory (**C:\MIST** by default) and extract files into this directory.

3. Running MIST

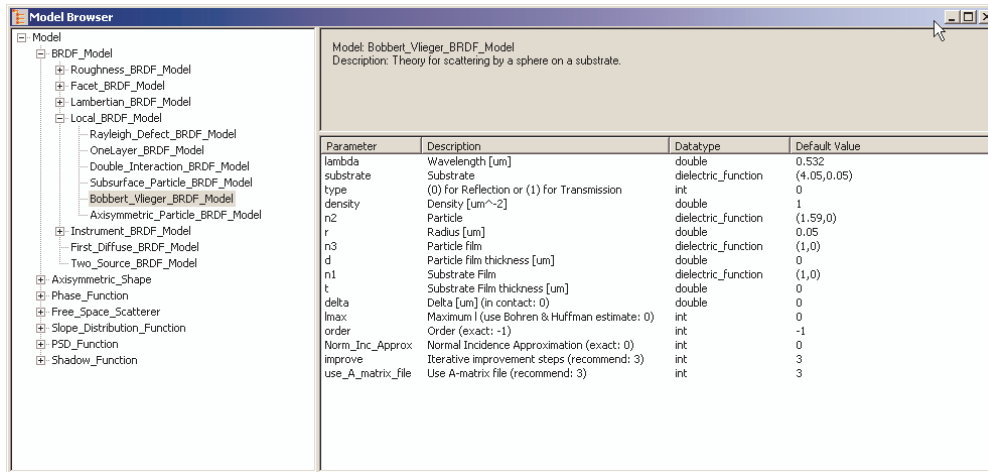
MIST is a 32-bit Windows* application. To run MIST, find the folder containing the executable program and double-click on its icon. You can create a shortcut to the program by right-clicking on the icon, then choosing “Create Shortcut.” The shortcut can then be moved to the Start Menu or the Desktop.

4. Model Browser

The Model Browser allows the user to view information about all the SCATMECH models and can be opened by selecting “Model Browser” from the menu. The window has three frames. The left frame provides a tree structure view of all of the SCATMECH model classes. The top right frame provides a synopsis of the model highlighted in the left frame. The bottom right frame provides a listing of all of the

* Certain commercial products are identified in this documentation in order to describe the software adequately. Such identification is not intended to imply recommendation or endorsement by the National Institute of Standards and Technology, nor is it intended to imply that the products are necessarily the best available for the purpose.

parameters, their descriptions, their data types, and their default values. More information about the models can be obtained from the SCATMECH documentation.



5. MIST Wizard Document

The MIST Wizard Document format is the preferred way to provide instructions for MIST to determine the integrated reflectance. A new document may be opened by selecting the menu item File→New and then selecting “MIST Wizard Document.” A saved document may be opened by selecting File→Open. A saved MIST Wizard Document will contain not only the instructions to generate the integrated reflectance, but also data from the last calculation. A document appears as a tree structure containing eight top level elements:

```

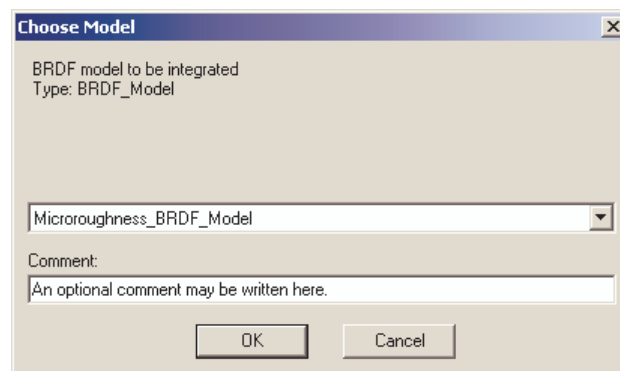
MODEL = ""
+ USER VARIABLES
+ REQUIRED VARIABLES
MODEL PARAMETERS
VARIED PARAMETERS
INTEGRALS
OUTPUTS
+ FILES

```

In the following subsections, each of these elements will be described in detail.

5.1 MODEL Wizard Element

The MODEL wizard element defines which SCATMECH BRDF model will be evaluated during integration. If you double-click on it, or select the element and press enter, a dialog box will open, which will allow you to choose a model from the selection of available models and provide a comment for annotating the document:



After pressing the OK button, the document will show the new model name, and will provide the model parameters with their default values in the MODEL PARAMETERS section (described in Sec. 5.4 below):

```

MODEL = Microroughness_BRDF_Model ; An optional comment may be written here.
+ USER VARIABLES
+ REQUIRED VARIABLES
- MODEL PARAMETERS
  lambda = 0.532
  substrate = [4.05,0.05]
  type = 0
  - psd = ABC_PSD_Function
    psd.A = 0.01
    psd.B = 362
    psd.C = 2.5

```

5.2 USER VARIABLES Section

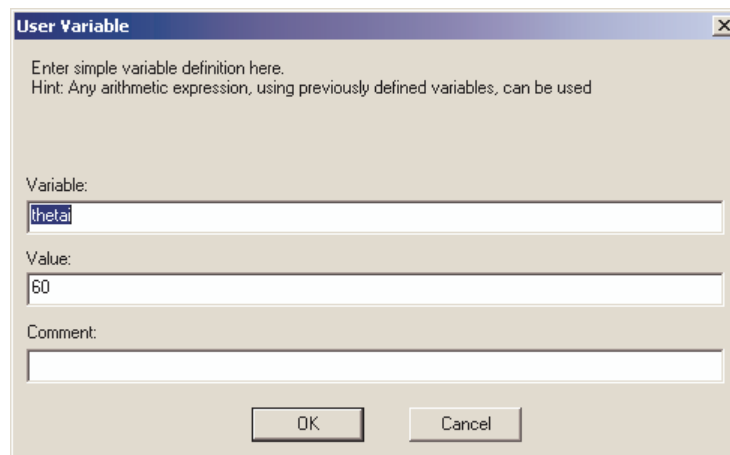
The USER VARIABLES section allows the user to define variables that can be used to make the calculation easier or more straightforward to the user. Some variables come predefined and are optional:

```

- USER VARIABLES
  pi = 4*atan(1)
  deg = pi/180
  thetai = 60
  thetas = 0
  inpol = 0

```

Other variables can be added, removed, edited, copied, or pasted by selecting any of the variables and right-clicking the mouse. The order of the variables may be changed by dragging any with the mouse or by selecting any and pressing CTRL and either the up button or the down button. If a new variable is being created or a current variable is being edited, then a dialog box will appear:



The dialog box titled "User Variable" contains the following fields and controls:

- Instruction: "Enter simple variable definition here. Hint: Any arithmetic expression, using previously defined variables, can be used"
- Variable: A text field containing "thetai"
- Value: A text field containing "60"
- Comment: An empty text field
- Buttons: "OK" and "Cancel"

The variable name can be any alphanumeric string containing no whitespace. The value can be any arithmetic expression using previously defined variables. See Sec. 9 below for further description of expressions.

5.3 REQUIRED VARIABLES Section

The REQUIRED VARIABLES section allows the user to define five parameters that are required during the calculation of integrated scatter:

```

- REQUIRED VARIABLES
  minsamples = 10
  differential = [2*deg]^2
  incidentangle = thetai*deg
  incidentpol = [1,cos[2*inpol*deg],sin[2*inpol*deg],0]
  rotation = 0*deg

```

The order of the required variables may be changed by dragging any with the mouse or by selecting any and pressing CTRL and either the up button or the down button. If the user double-clicks on any of these parameters, a dialog box will open, allowing the user to edit the parameter value. The interpretation of each variable is defined below:

DIFFERENTIAL – The approximate differential solid angle (in steradians) used during the integration. The smaller this value, the longer the calculation will take, but the more accurate the results will be. A reasonable value for a fast calculation can be obtained by a value of 0.001, which corresponds to a grid spacing of about $2^\circ \times 2^\circ$.

MINSAMPLES – The minimum number of samples for any integration. If the solid angle of the integration is small compared to **DIFFERENTIAL**, then the program will use a smaller differential solid angle. It is best to set this value to about 10.

INCIDENTANGLE – The incident angle (in radians) of the incoming light.

INCIDENTPOL – The Stokes vector intensity for the incident light. The Stokes vector should have a unit intensity in order for the results to be interpreted as a reflectance. Common incident Stokes vectors are shown in the table below:

(1,0,0,0)	unpolarized incident light
(1,-1,0,0)	p-polarized incident light (E-field in the plane of incidence)
(1,1,0,0)	s-polarized incident light (E-field perpendicular to the plane of incidence)
(1,0,1,0)	45° polarized incident light
(1,0,0,1)	left-circularly polarized incident light

ROTATION – The rotation angle (in radians) of the sample about the surface normal. If this parameter is zero, then the light is incident along the fiducial direction of the model. If the scattering model is for an isotropic surface, this parameter is ignored.

5.4 MODEL PARAMETERS Section

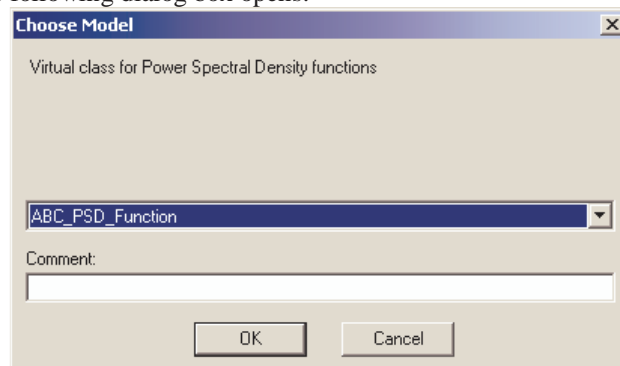
The MODEL PARAMETERS Section lists the parameters in the model, allowing the user to edit them:

```

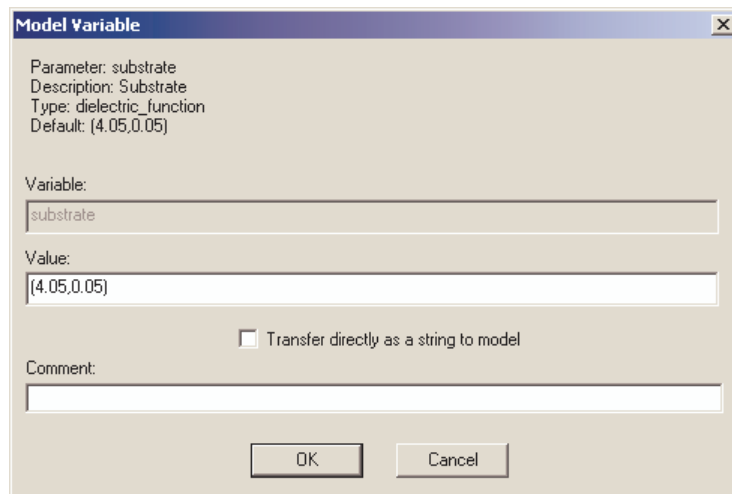
MODEL PARAMETERS
├── substrate = (4.05,0.05)
├── type = 0
├── lambda = 0.532
└── psd = ABC_PSD_Function
    ├── psd.A = 0.01
    ├── psd.B = 362
    └── psd.C = 2.5

```

Some parameters are models themselves and may have sub-parameters. For example, if the user double clicks on **psd** above, the following dialog box opens:



The user can then select among the possible models for that parameter. When the user presses OK, all of the sub-parameters are updated with their default values. Double-clicking on other parameters will open the following dialog box:



Model Variable

Parameter: substrate
 Description: Substrate
 Type: dielectric_function
 Default: (4.05,0.05)

Variable:

Value:

☐ Transfer directly as a string to model

Comment:

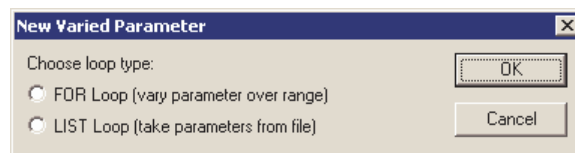
OK Cancel

If the box marked “Transfer directly as a string to model” is not checked, then any arithmetic expression may be used for the value, using any parameters defined above it, and that the parameter may be used in other expressions. Some parameters should not be evaluated or treated as variables, namely those that require a filename, such as dielectric stack information. Expressions can be used inside complex numbers (that is, as two expressions separated by a comma and surrounded by parentheses). However, if a filename is used for a dielectric function, this box should be checked, so that MIST does not attempt to evaluate it as a numeric expression.

5.5 VARIED PARAMETERS Section

The VARIED PARAMETERS section allows the user to specify parametric variation of any numeric parameter. There are two different types of varied parameter elements: the FOR loop and the LIST loop. The FOR loop allows a parameter to be varied from a starting value to an ending value with an increment, while a LIST loop allows the user to specify a file which tabulates the parameter values for which the calculation is to be performed.

To add an element to this section, the user should select the VARIED PARAMETERS Section, right-click on the mouse, and select Add. A dialog box will open to allow the user to specify the loop type:



New Varied Parameter

Choose loop type:

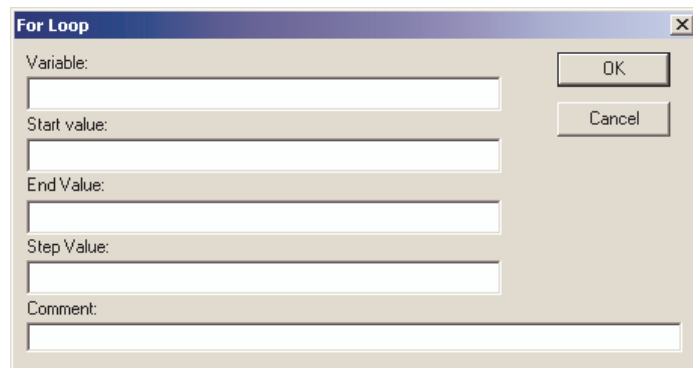
☐ FOR Loop (vary parameter over range)

☐ LIST Loop (take parameters from file)

OK Cancel

5.5.1 FOR loop

A FOR loop enables the user to specify the variable, its range, its increment, and a comment. If a FOR loop is chosen, a dialog box will appear:



For Loop

Variable:

Start value:

End Value:

Step Value:

Comment:

OK Cancel

The variable may be any numeric variable defined in the USER VARIABLES, REQUIRED VARIABLES, or MODEL PARAMETERS sections. The start value, the end value, and the step value may be any expression, using any of the variables.

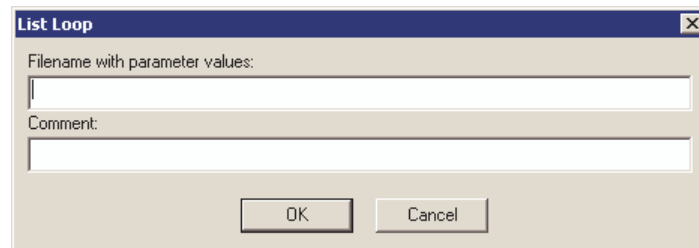
The order of multiple For Loops may be changed by dragging the items in the tree menu. The first one listed is the most slowly varying parameter, while the last is the most rapidly changing parameter.

After For Loops have been defined, they will be shown in the FOR LOOPS section of the tree menu. For example:



5.5.2 LIST loop

A LIST loop enables the user to specify a file, which contains a list of parameters and the values that they should take. If a LIST loop is chosen, a dialog box will appear:



The file should be a text file containing whitespace-delimited columns. The first line should specify the parameters that should be varied, and the remaining lines should contain the values that those parameters should take. For example:

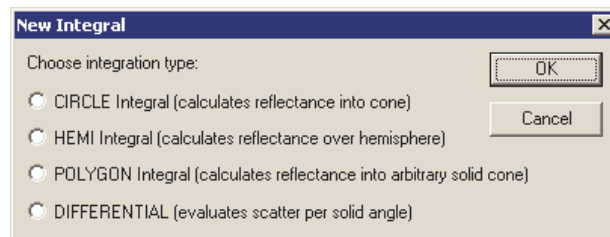
thetai	thetas
25	-10
25	0
25	10
30	20
30	30
30	40

The variable may be any numeric variable defined in the USER VARIABLES, REQUIRED VARIABLES, or MODEL PARAMETERS sections. In this example, six different combinations of thetai and thetas would be used. After a LIST loop has been defined, it will show up in the VARIED PARAMETERS section of the tree menu. For example:



5.6 INTEGRALS Section

The INTEGRALS section defines the integrals that will be evaluated by the program. There are four different types of integrals, HEMI, CIRCLE, POLYGON, and DIFFERENTIAL. Each integral must be given a unique name. To add a new integral, the user must select the INTEGRALS section, right-click on the mouse, and select Add. A dialog box will open enabling the user to choose one of the four types of integrals:



Once the user has defined the integrals, they will be shown on the tree menu as such:

```

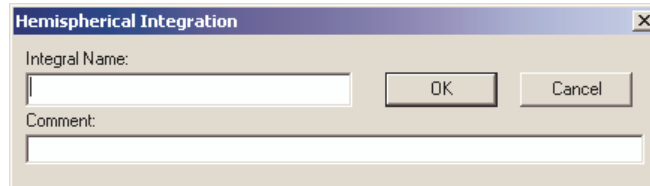
INTEGRALS
  integ1 = DIFFERENTIAL (double click to view)
  integ2 = CIRCLE (double click to view)
  integ3 = HEMI (double click to view)
  integ4 = POLYGON (double click to view)

```

Each integral type is described in the following subsections:

5.6.1 HEMI Integral

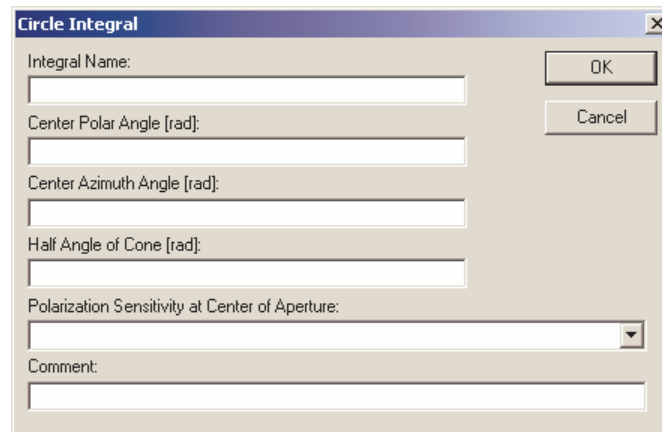
A HEMI integral calculates the reflectance over the entire hemisphere. It has no parameters, other than its name, and does not allow for any polarization sensitivity. The dialog box that opens when the user selects a HEMI integral is shown below:



The dialog box titled "Hemispherical Integration" contains two input fields: "Integral Name:" and "Comment:". To the right of the "Integral Name:" field are "OK" and "Cancel" buttons.

5.6.2 CIRCLE Integral

A CIRCLE integral integrates the reflectance into a right circular cone centered on a specified direction, having a specified half angle and polarization sensitivity. The polarization sensitivity is given as a four-element Stokes vector. The dialog box that opens when the user selects a CIRCLE integral is shown below:



The dialog box titled "Circle Integral" contains several input fields: "Integral Name:", "Center Polar Angle [rad]:", "Center Azimuth Angle [rad]:", "Half Angle of Cone [rad]:", "Polarization Sensitivity at Center of Aperture:" (with a dropdown arrow), and "Comment:". To the right of the "Integral Name:" field are "OK" and "Cancel" buttons.

All of the angles must be specified in radians. By default, the variable "deg" is defined to enable one to convert a value in degrees to one in radians. Thus, "45*deg" is $\pi/4$ radians.

5.6.3 POLYGON Integral

Any arbitrary shape may be specified using a POLYGON integral. When a user selects POLYGON integral, the following dialog box opens:

Polygon Integral

Integral Name:

OK Cancel

Direction for which polarization is defined:

Theta [rad]: Phi [rad]:

Polarization Sensitivity:

Polygon Vertices:

Theta [rad]: Phi [rad]:

Change Add Remove Move Up Move Down

Theta [rad] Phi [rad]

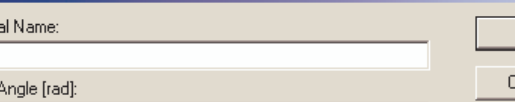
Comment:

The user must choose a direction by which the polarization is defined and a sensitivity for polarization in that direction. If the integral is to be performed without any polarization sensitivity, the direction can be set to $\theta = 0$ and $\phi = 0$, and the polarization sensitivity can be set to (1,0,0,0).

The vertices of the polygon can be entered by entering directions into the Theta and Phi edit boxes, and pressing the Add button. The direction will show up in the list box. Once in the list box, a particular direction can be highlighted and edited, removed, moved up in the list, or moved down in the list.

5.6.4 DIFFERENTIAL Integral

The DIFFERENTIAL integral is not a true integral. It evaluates the reflectance per solid angle in a specified direction. When a user specifies a DIFFERENTIAL integral, the following dialog box opens:



Differential [X]

Integral Name: OK

Polar Angle [rad]: Cancel

Azimuth Angle [rad]:

Polarization Sensitivity ▼

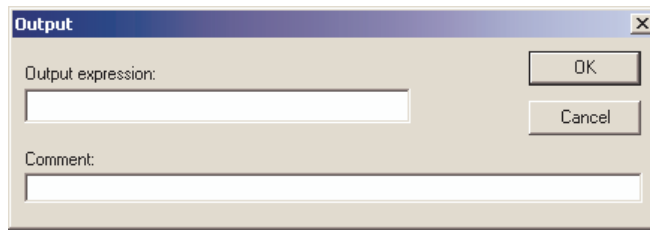
Comment:

All of the angles must be specified in radians.

5.7 OUTPUTS Section

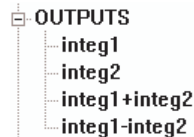
The OUTPUTS Section defines what quantities are stored and written to the output file for each set of integrals. Generally, they would include all of the integral values specified in the INTEGRALS sections, but may also include arithmetic combinations of them or other variables defined the preceding sections. To

choose a new output, the user selects the OUTPUTS section, right-clicks on the mouse, and selects “New”. The following dialog box will open:



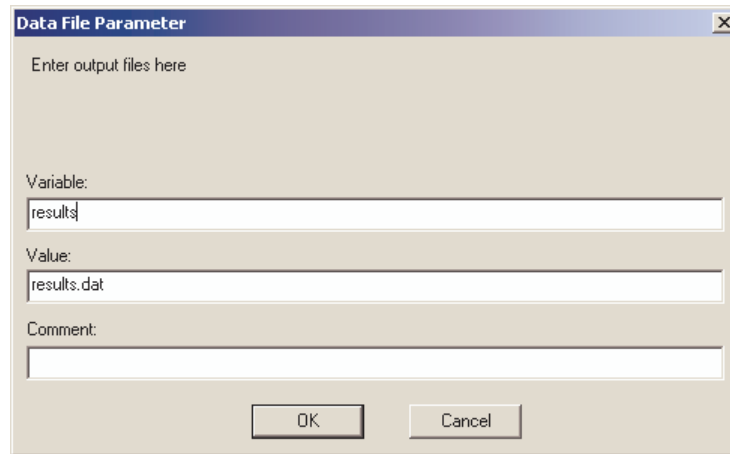
The 'Output' dialog box has a title bar with a close button. It contains two text input fields: 'Output expression:' and 'Comment:'. To the right of the 'Output expression:' field are two buttons: 'OK' and 'Cancel'.

After a number of elements have been added, the tree menu will show them:



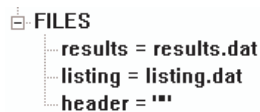
5.8 FILES Section

The FILES section allows the user to specify where the results will be written. When one adds or edits an element in this section, a dialog box opens:



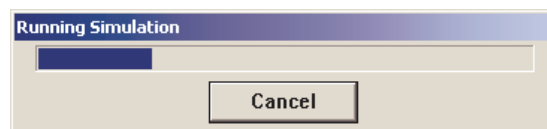
The 'Data File Parameter' dialog box has a title bar with a close button. It contains a large text area at the top with the label 'Enter output files here'. Below this are three text input fields: 'Variable:', 'Value:', and 'Comment:'. At the bottom are two buttons: 'OK' and 'Cancel'.

There are three different variables allowed in this section: results, listing, and header. The results variable is used to specify the output data file. The listing variable is used to specify a data file for other information that sometimes can help in debugging a simulation. The header variable is used to define information that is placed at the top of the output data file. Multiple header variables (simply repeating the header definition) can be used.



6. Running the Simulation

To begin a simulation, the user should select “Simulate” from the main menu. A progress bar will appear:



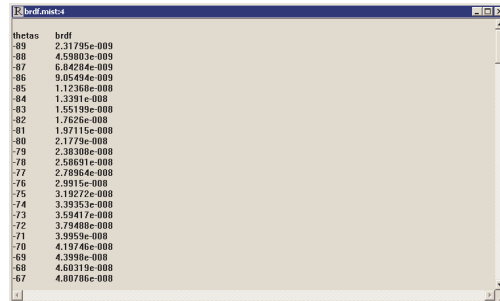
The 'Running Simulation' dialog box has a title bar. It contains a progress bar with a blue fill. Below the progress bar is a 'Cancel' button.

The user may cancel a simulation by pressing the “Cancel” button. However, it may take awhile for the program to acknowledge that it must stop.

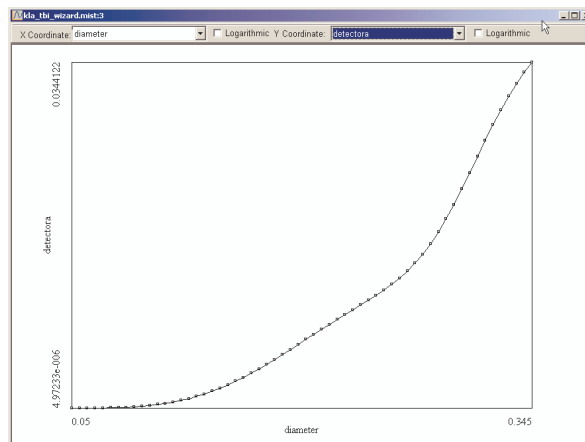
7. Viewing the Results

There are three different ways to view the output. First, one can use a spreadsheet application to read the file specified by the RESULTS item of the FILES section. Secondly, one can view the contents of this file in a text window supplied by MIST. Finally, a rudimentary graph can be displayed, showing the outputs as a function of the parametric variables.

To view the contents in a text window, select View→View Results (Text) from the main menu. This view is useful when one wants to see the specific numbers.



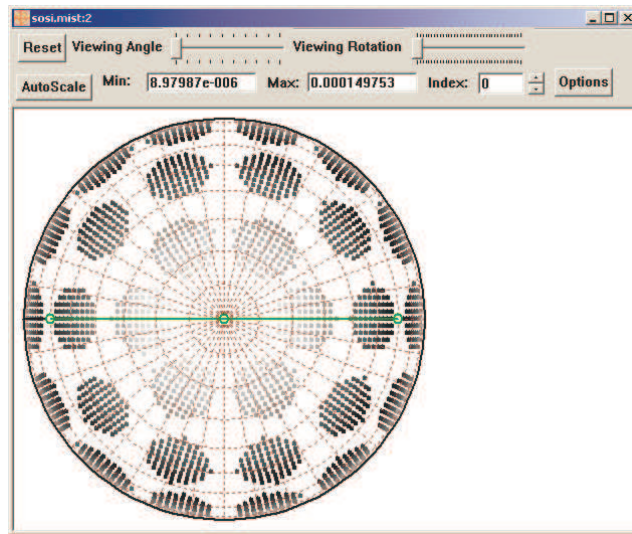
To view a graph of the results, select View→View Results (Graph) from the main menu. A window opens up showing the data as a function of the variable(s) defined in the FOR loops.



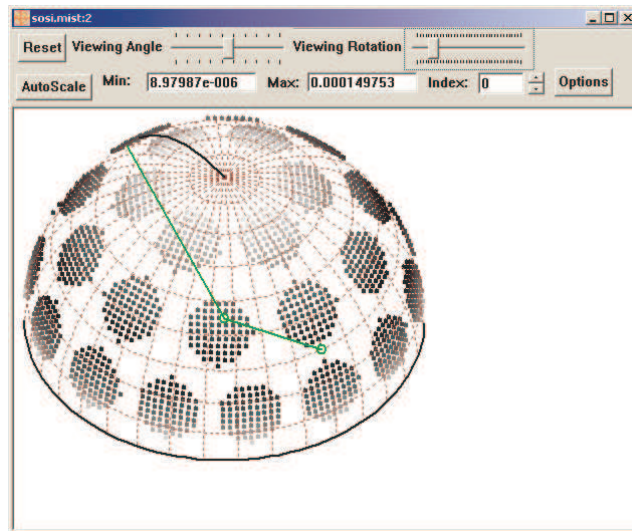
The results may be plotted against linear or logarithmic axes.

8. Viewing the Sampled Points

For several reasons, it is often useful to view the sampled points. For example, one can check to see that the integration region matches that which is anticipated. Also, one might wish to see where the intensity is strongest on a detector, and where it is weakest. For these reasons, MIST provides a view of the scattering hemisphere with the integrations points shown with their intensities. To view the sampled points, select View→View Sampled Points from the main menu. A window will appear:



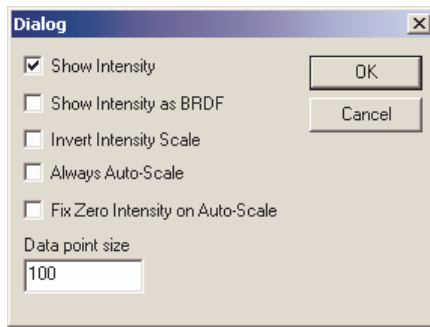
By default, the integration points are shown over the scattering hemisphere as viewed from the surface normal. By sliding the viewing angle and the viewing rotation slider bars, the direction over which the hemisphere is viewed can be changed:



The incident plane is shown with a dark curve starting at the surface normal. The incident and specular beams are shown with green line segments, and the points that the incident and specular beams intersect the hemisphere and the sample are shown as circles.

Index refers to the step index of the FOR loop. By changing the index, one can view the intensity or the shape of the integration domain as a function of the varying parameter.

By pressing the Options button, some parameters used for displaying the sampled points can be changed:



Show Intensity—Checking this box will show the integration points with points whose gray scale depends upon the intensity, while un-checking it will show the integration points in black.

Show Intensity as BRDF—Checking this box will show the gray scale (if the Show Intensity box is checked) corresponding to BRDF, while un-checking it will show it corresponding to intensity.

Invert Intensity Scale—Checking this box will make the gray scale be whiter when the intensity is higher, while un-checking it will show the more intense points darker.

Always Auto-Scale—Checking this box will ensure that anytime the image changes (due to calculation or looking at a different step), that the results will be auto-scaled over the range of intensities.

Fix Zero Intensity on Auto-Scale—Checking this box will set the lowest intensity scale to zero, while un-checking it will set the bottom of the scale to the lowest intensity shown.

Data point size—This parameter sets the size of the circles used to show the integration points. By default, this value is 100. One can effectively show a map of intensity by setting this number so that the points fill the gaps between adjacent points.

9. Expressions

All parameters in MIST are treated as expressions which are evaluated each time they are needed. These expressions can use any of the binary arithmetic operators listed below, listed in order of precedence, with each row indicating items having the same precedence:

x^y	power				
$x*y$	multiplication	x/y	division		
$x+y$	addition	$x-y$	subtraction		
$x>y$	greater than	$x<y$	less than	$x=y$	equal to
$x\&y$	and	$x y$	or		

Parentheses can be used and nested to any degree. The table below lists functions which can be used in the expressions:

Exp(x)	Exponential	Log(x)	Natural logarithm
Log10(x)	Base-10 logarithm	Sqrt(x)	Square root
Sin(x)	Sine	Sind(x)	$\sin(x*\pi/180)$
Cos(x)	Cosine	Cosd(x)	$\cos(x*\pi/180)$
Tan(x)	Tangent	Tand(x)	$\tan(x*\pi/180)$
Asin(x)	Arc-Sine	Asind(x)	$\text{Asin}(x)*180/\pi$
Acos(x)	Arc-Cosine	Acosd(x)	$\text{Acos}(x)*180/\pi$
Atan(x)	Arc-Tangent	Atand(x)	$\text{Atan}(x)*180/\pi$
Sinh(x)	Hyperbolic Sine	Cosh(x)	Hyperbolic Cosine
Tanh(x)	Hyperbolic Tangent	Atan2(y,x)	Polar angle of the point (x,y)
Atan2d(y,x)	$\text{Atan2}(y,x)*\pi/180$		

10. Accuracy

While most of the BRDF models contained in the SCATMECH library are based upon physical principles, most are approximations that have a limited range of accuracy. It is up to the user to assess the accuracy of each model to determine if the results he or she obtains are of quantitative value or are just qualitative guides to data trends.

Aside from the intrinsic accuracy of the particular model, the accuracy of the integration depends upon the values of the variables **SOLIDANGLE** and **MINSAMPLES**, any structure in the scattering within the integration solid angle, and the shape of the integration solid angle. The program chooses the number of sampled points by dividing the solid angle of a right circular cone that circumscribes the integration solid angle by the variable **SOLIDANGLE**, assuring that this value is above **MINSAMPLES**. It then samples directions on a square grid within this right circular cone. If the point is outside of the integration solid angle, it returns zero intensity for that direction. The results are adjusted by the ratio of the calculated projected solid angle (as determined by the sampled points) and the actual projected solid angle of the desired shape, as determined by a path integral around the perimeter.

11. Examples and Other Notes

11.1 Specifying material properties

In all of the examples, complex material indices of refraction are specified by constant values. The SCATMECH library, however, allows the use of external files which contain the optical constants as functions of wavelength. Such a file should be a text file containing three tab-delimited columns, in which the first column represents the wavelength, the second column the index of refraction, and the third column the absorption coefficient. The optical properties of the substrate, for example, can then be specified by the following model parameter declaration

```
MODEL PARAMETERS
  substrate = silicon.txt
```

The “Transfer directly as a string to model” box must be checked, or MIST will try to interpret “silicon.txt” as a numeric expression. In this manner, the VARIED PARAMETERS section statement

```
VARIED PARAMETERS
  FOR lambda FROM 0.2 TO 0.8 BY 0.02
```

will allow the reflectance to be calculated over a variety of wavelengths even though the optical properties of the substrate are wavelength dependent.

11.2 Use of Local BRDF Models

Any of the SCATMECH models which inherit the class **Local_BRDF_Model** (such as **Bobbert_Vlieger_BRDF_Model** or **Rayleigh_Defect_BRDF_Model**) calculate the differential scattering cross-section (DSC) rather than the BRDF. The class **Local_BRDF_Model** uses the parameter **density** to convert the DSC to BRDF. If one is interested in the integrated cross section for an isolated particle or defect, then one should set this parameter by

```
MODEL PARAMETERS
  density = cos(incidentangle)
```

If, instead, one is interested in a net effective reflectance, when the effective beam area is **area**, then one should set this parameter by

```
MODEL PARAMETERS
  density = cos(incidentangle)/area
```

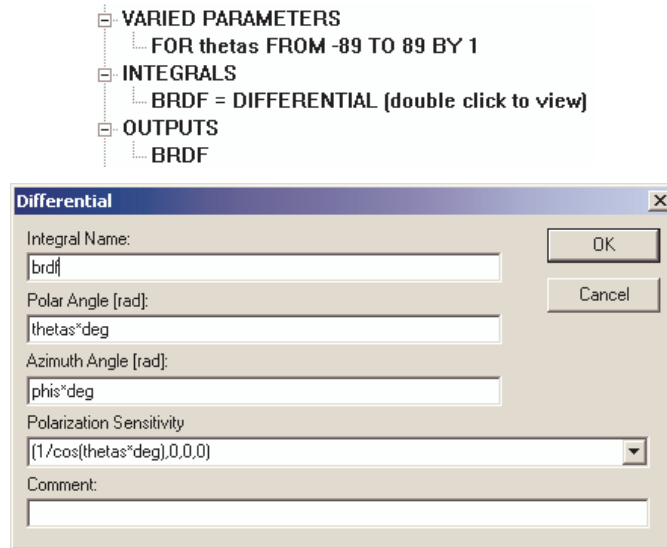
11.3 Calculated Integrated Scatter by Isolated Particles

While MIST was not designed with isolated particles in mind, with a little insight and knowledge of the SCATMECH models, it can effectively be used for that. If the incident angle is 90°, the transmission hemisphere will be symmetric with the reflection hemisphere. The subsurface sphere model effectively performs the scattering by a free space sphere embedded in a transparent substrate, and that substrate can

be set to have a unit index. Since the model calculates the BRDF, before calculating differential reflectance, the incident angle must be set to a value close to, but not equal to 90° . The example code in **particle.mist** illustrates this procedure.

11.4 Calculating BRDF

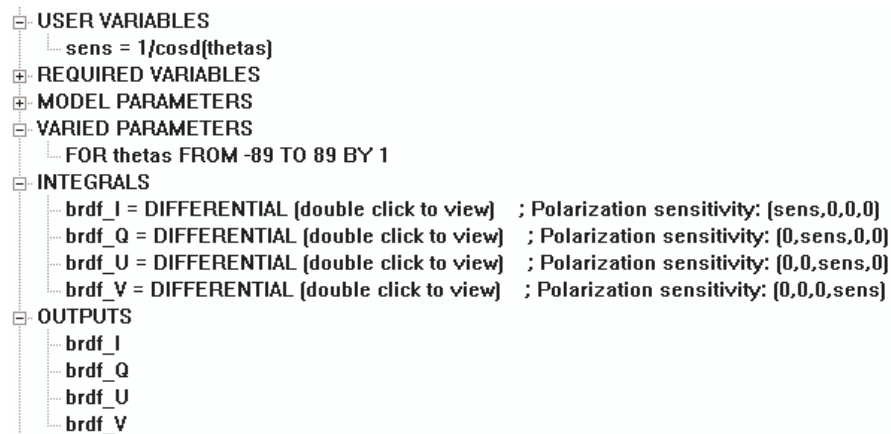
MIST can be used to calculate BRDF by using a DIFFERENTIAL integral, using a sensitivity of $1/\cos(\theta_s)$:



The example code **brdf.mist** can serve as a template for BRDF calculations.

11.5 Calculating Stokes Vector BRDF

Stokes vector BRDF may be calculated using four differential integrals, each with sensitivity to a different element:



The example code **stokes_brdf.mist** can serve as a template for Stokes vector BRDF calculations.

11.6 Calculating Mueller Matrix BRDF

Mueller matrix measurements can be obtained as for Stokes vector BRDF measurements by looping through an index that selects the incident Stokes vector:

```

USER VARIABLES
  inpol = 1
  sens = 1/cosd(thetas)
REQUIRED VARIABLES
MODEL PARAMETERS
VARIED PARAMETERS
  FOR phis FROM 0 TO 180 BY 5
  FOR inpol FROM 1 TO 4 BY 1
INTEGRALS
  brdf_I = DIFFERENTIAL (double click to view) ; Polarization sensitivity: {sens,0,0,0}
  brdf_Q = DIFFERENTIAL (double click to view) ; Polarization sensitivity: {0,sens,0,0}
  brdf_U = DIFFERENTIAL (double click to view) ; Polarization sensitivity: {0,0,sens,0}
  brdf_V = DIFFERENTIAL (double click to view) ; Polarization sensitivity: {0,0,0,sens}
OUTPUTS
  brdf_I
  brdf_Q
  brdf_U
  brdf_V

```

The example code **mueller_brdf.mist** can serve as a template for Mueller matrix BRDF calculations.

11.7 Calculating Integrated Cross Section for Particles on Surfaces

One application of MIST is to develop response curves for light-scattering-based particle scanners. These devices have a relatively collimated beam incident on a sample and collect scattered light over a relatively large set of directions. The scattered signal is often attributed to the presence of particles, and the signal can be correlated with the size of the particle. It is often useful to estimate the signal that one would expect for different sphere sizes. The example code **scanner.mist** is an example of such a calibration, using the Bobbert-Vlieger theory for scattering by a sphere on a surface. The code integrates the scatter between polar angles **narrow** = 25° and **wide** = 70° for particle diameters from 0.05 μm to 0.350 μm.

12. Legal Disclaimer

The MIST and SCATMECH software packages were developed at the National Institute of Standards and Technology by employees of the Federal Government in the course of their official duties. Pursuant to Title 17 Section 105 of the United States Code this software is not subject to copyright protection and is in the public domain. MIST and SCATMECH are experimental systems. NIST assumes no responsibility whatsoever for its use by other parties, and makes no guarantees, expressed or implied, about its quality, reliability, or any other characteristic. We would appreciate acknowledgment if the software is used. This software can be redistributed and/or modified freely provided that any derivative works bear some notice that they are derived from it, and any modified versions bear some notice that they have been modified.

13. Registering MIST

Registration of the NISTMIST program is voluntary and enables you to be notified when new versions are released. It also enables you to provide feedback that helps us improve the library and its documentation. To register, send an e-mail message to thomas.germer@nist.gov, indicating your interest in registering your copy of the software.

14. Version History

14.1 Version 1.00

Version 1.00, the original version of MIST, was released in June 2004.

14.2 Version 2.00

Version 2.00 was released in July 2005 and represented a major upgrade. The program was changed to include a graphical user interface and was linked with SCATMECH version 5.00.

14.3 Version 2.10

Version 2.10 was released in August 2005 and represents a minor bug fix to MIST and SCATMECH. The rotation of the polarization sensitivity over a finite solid angle was miscalculated in previous versions. This version was linked with SCATMECH version 5.01.

14.4 Version 2.20

Version 2.20 was released in July 2006 and represents a minor bug fix to MIST and SCATMECH. Prefix negative signs in some expressions were not handled correctly. This version was linked with SCATMECH version 5.02.

14.5 Version 2.30

Version 2.30 was released in August 2006 and represents a minor bug fix to MIST and SCATMECH. The BRDF sampling file capability was restored, and file writing was significantly sped up. This version was linked with SCATMECH version 5.03.

APPENDIX

Figure 3 provides a graph of the spherical coordinates of the reflectance hemisphere. This diagram is useful for planning calculations.

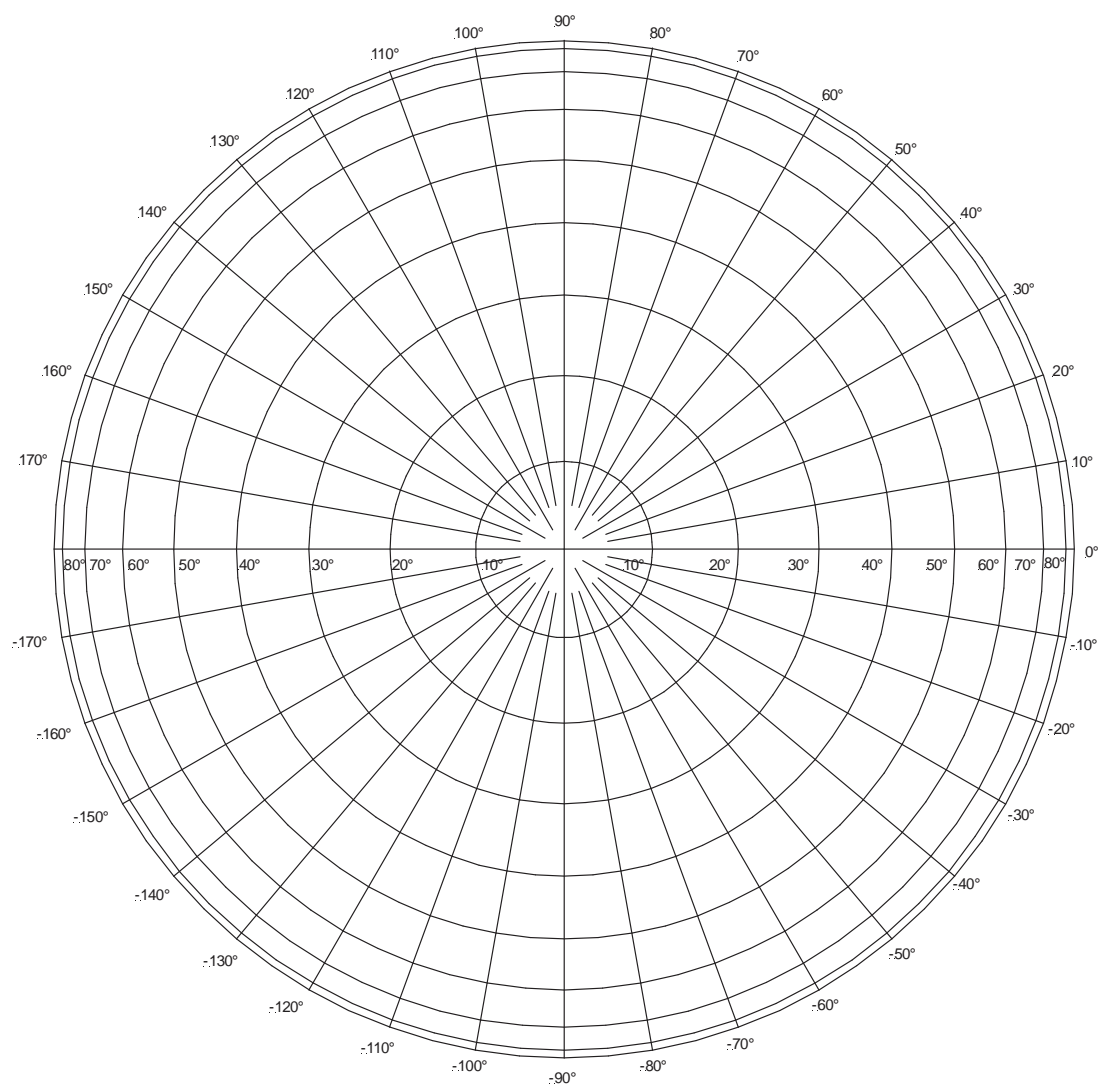


FIGURE 3 The reflectance hemisphere.